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THE DETUMBLING OF AN AXIALLY SYMMETRIC

SATELLITE WITH AN ORBITAL MANEUVERING

VEHICLE BY NONLINEAR FEEDBACK CONTROL

THESIS

Kirk R. Fleming First Lieutenant, USAF AFIT/GA/AA/85D-5

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THESIS

Presented to the Faculty of the School of Engineering
of the Air Force Institute of Technology
Air University

In Partial Fulfillment of the
Requirements for the Degree of
Master of Science in Astronautical Engineering

Kirk R. Fleming, B.S.

First Lieutenant, USAF

December 1985

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Abstract

Symmetric satellite is considered. Detumbling is achieved with another axisymmetric orbital maneuvering vehicle (OMV) joined to the target satellite with a universal joint. The joint provides two rotational degrees of freedom and is translated across the surface of the OMV during the detumbling process. The target satellite and the OMV with its three momentum wheels are modelled as a five body system using Eulerian-based equations of motion developed by Hooker and Margulies. A Liapunov technique is applied to derive a nonlinear feedback control law which drives the system asymtotically to a final spin-stabilized state. State and control histories are presented and indicate that the dtumbling process is benign. Constraint force and moment loads at the connection between the OMV and target satellites are also presented, and indicate that no extreme loads are encountered during the despinning and detumbling process.

Notation

mass of body λ m λ total system mass inertia dyadic of body λ about its mass center angular velocity of body λ $\overline{\omega}_{\lambda}$ non-gravitational external force on body λ non-gravitational external torque on body λ geocentric position vector for mass center of body $\boldsymbol{\lambda}$ interaction force acting on body λ through joint j constraint torque acting on body λ through joint j unit dyadic gravitational constant geocentric position vector for system center of mass unit vector in direction of $ar{
ho}$ = spring-damper torque acting on body λ at joint j unit vector along rotation axis of joint i ĝ

angle of rotation about axis \hat{g}_i

angular velocity of the reference body (the OMV)

 γ_{i}

 $\overline{\omega}_0$

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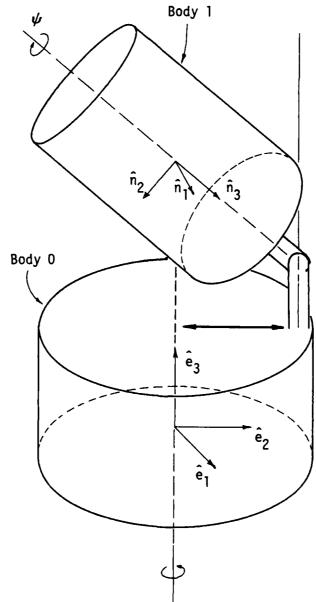
THE DETUMBLING OF AN AXIALLY SYMMETRIC SATELLITE WITH AN ORBITAL MANEUVERING VEHICLE BY NONLINEAR FEEDBACK CONTROL

I. Introduction

The service or repair of orbiting satellites beyond direct reach of the Space Shuttle may require an orbital maneuvering vehicle (OMV) to rendezvous and dock with the target satellites. If the target is spinstabilized it may be necessary to despin it. If the target has experienced control system malfunction or for some reason is not in pure spin, it may be ecessary to detumble it. Docking followed by despinning or detumbling is defined here as capture. Docking is accomplished by first driving a grappling device on the OMV to a state of rest relative to some docking point on the target. The OMV and target can ther be connected. Despinning or detumbling is accomplished by applying torques to the target through the connecting joint while firing the OMV thrusters to control the absolute motion of the two-body system. Widhalm and Conway derived a feedback control law (1) which solved the despinning/detumbling problem for the case of axisymmetric target and OMV satellites. They used a connecting joint which could translate across the surface of the OMV. The translational degree of freedom of the joint is depicted in Fig. 1 by the double arrow. The ability to translate the joint provides for joint position adjustment during docking, and allows the joint to be driven to the OMV axis of symmetry during detumbling. The resulting configuration can then be spin-stabilized.

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This thesis extends the Widhalm and Conway model to include three orthogonal momentum wheels on the OMV, and develops a feedback control



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Fig. 1. The Conway and Widhalm Model for the Two Body Satellite

law to couple the momentum wheel torques to the system state. The target satellite docked with the OMV and its three momentum wheels are modelled as a system of five rigid, constant mass bodies. The control problem is formulated by defining the system initial configuration and the desired final state, and by deriving the equations of motion.

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II. Problem Formulation

System Configuration

An axisymmetric target satellite is docked with an OMV which, with its three orthogonal momentum wheels, is also axisymmetric (see Fig. 2). The target and OMV are connected with a universal joint having two rotational degrees of freedom and the capability of translation across the surface of the OMV. The translational degree of freedom is depicted in Fig. 2 by the bold double arrow. The center of mass of the target lies on the $\ddot{\text{b}}_3$ axis as does the mass center of the OMV-momentum wheel combination. The OMV is in a state of pure spin about \hat{b}_3 , and the target is in a state of spin with precession about \hat{b}_3 at a rate equal to the OMV spin rate. With no external moments or forces acting on the system a dynamically stable configuration results. This configuration represents the initial state of the system. The detumbling and despinning process is complete when the joint has been driven to a position lying on the $\mathbf{b_3}$ axis, and the target spin rate relative to the OMV is zero with the OMV itself still in a state of pure spin about the $\hat{\mathbf{b}}_3$ axis. This configuration, or one arbitrarily close to it, represents the desired final state of the system. Both the initial and final states as defined imply that the initial and final angular velocities of the momentum wheels having rotational freedom about the $\hat{\mathbf{b}}_1$ and $\hat{\mathbf{b}}_2$ axes are zero. The initial and final angular velocity of the \dot{b}_3 wheel is arbitrary.

The Hooker-Margulies Equations

The dynamical attitude equations for a two-body satellite were derived by Fletcher, Rongved and Yu (2), and were generalized for an

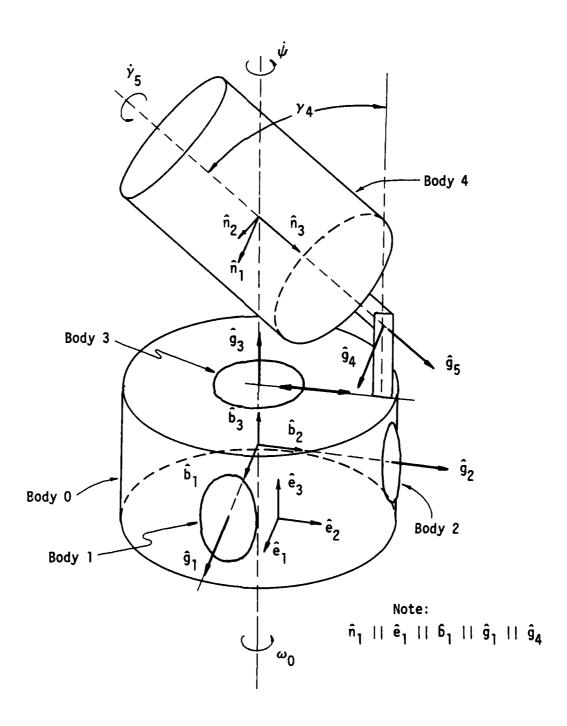


Fig. 2. The Five-Body Satellite Model

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complete derivation is a set of 3n scalar equations for an n-body system. The equations are free of the unknown joint constraint forces, but still contain the unknown constraint torques (3:125).

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Hooker (4) showed in a subsequent paper that the constraint torques could also be explicitly eliminated. The equations derived in reference (3) are written for all the bodies Tying on one side of a selected joint and subsequently added. The interaction torques all cancel in pairs, with the exception of the constraint torque at the free joint. If the selected joint has a rotational degree of freedom about an axis g, the dot product of g and the expression just found for the torque is zero. Writing the dot product and setting it to zero yields an equation free of the constraint torque. Repeating the process for each degree of freedom at each joint eliminates all the unknown constraint torques and yields a system of r equations for an n-body system having r rotational degrees of freedom. These equations are referred to in some of the references as the modified Hooker-Margulies equations.

Although for an identical dynamical system a Lagrangian derivation would provide the same number of equations as the HM equations, the resulting expressions would not be written in terms of the physical body axes, as are the HM and modified HM equations. As a result adaptation to active control and modification to include effects such as joint motion would be more difficult (4:1205). The modified HM equations significantly reduce the required computer time for solution due to the reduction in the number of equations from 3n to r.

The constraint torques at the joints were eliminated explicitly by taking the dot product of the unit vector about which the joint is

n-body system by Hooker and Margulies (3). Both derivations assume that the bodies are connected by joints which are fixed with respect to the bodies they connect. In addition, the generalized Hooker-Margulies (HM) equations assume that the bodies are connected in a topological tree. This means that there are no closed loops formed by the interconnected bodies. The restriction of immoveable joint is removed in an extension of the HM equations which will be discussed later. The extended equations then apply to the OMV-target satellite system when modelled as a system of five interconnected rigid bodies.

The derivation of the HM equations begins with the Newton and Euler equations for an n-body system. Each of the two sets of equations contains force terms representing the unknown constraint reactions which occur at the joints between adjacent bodies. An expression for each joint constraint force can be isolated by writing Newton's equations for all the bodies that lie to one side of any selected joint. The equations are added together, with the result that all the interaction forces canin pairs with the exception of the constraint force occurring at the selected joint. Repeating the process for all the joints in the system yields expressions for all the unknown constraints in terms of the system external forces and in terms of the inertial accelerations of each body in the system.

The joint constraint forces appear in Euler's equations as torques about the individual body mass centers, and can be replaced by the expressions for the constraints obtained in the process described. The result is the original Euler equations for the system, but with the unknown joint interactions explicitly eliminated. The result of the

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free to rotate (there may of course be more than just one) with the summed vector dynamical equations for the bodies that lie to one side of that joint. The value of the constraint torque can be computed after the modified HM equations are solved, however. Given the system state, the derivatives of the state variables can be computed using the modified HM equations. All the variables in the equation which was dotted with the joint degree of freedom vector \hat{g} are then known, and can all be brought to one side of the equation with the resulting sum equalling the scalar components of the constraint torque (4:1207).

The interaction force at the joints can be computed by finding the accleration of the mass center of the system of bodies lying to one side of a joint (relative to the system mass center) and multiplying by the total mass of that subsystem. For the case of no external forces, the product is the vector constraint force acting at the selected joint.

Application of the HM Equations

The Eulerian-based equations of motion for multi-body systems given by Hooker and Margulies (3) and modified by Hooker (4) are restricted to those systems of bodies connected in such a way that no closed loops are formed, and do not account for motion of the joints relative to the bodies adjacent to the joint. This last restriction was removed in an extension of the modified HM equations by Conway and Widhalm (5) to permit the translation of the joint across the face of the OMV. Thus the extended equations can be applied to the OMV, momentum wheels and target satellite system under consideration. Referring to Fig. 2 the OMV is labelled body 0, with the b basis fixed at its geometric center. The geometric center of the OMV is chosen to coincide with the center of mass

of the OMV-momentum wheel composite. That is, remove the target from the system and the system center of mass then lies at the origin of the \hat{b} frame. The momentum wheels lying on axes \hat{b}_1 , \hat{b}_2 , and \hat{b}_3 are labelled bodies 1, 2, and 3 respectively. The target satellite is body 4. The \hat{e} basis is fixed in body 0 at its mass center, and the \hat{n} basis is fixed in the target at its mass center. Since the target is precessing about its own angular momentum vector at a rate, $\hat{\psi}$, the OMV is positioned relative to the target so that the target's center of mass and angular momentum vector both lie on the \hat{b}_3 axis. The OMV is then spun about \hat{b}_3 at the same rate, $\hat{\psi}$, the target precession rate. The cone angle, γ_4 , and the distance from the target center of mass to the joint determine the required position of the joint on the OMV face for docking. The target's cone angle, γ_4 , precession rate, $\hat{\psi}$, spin rate, $\hat{\gamma}_5$, and mass properties are related as shown by Greenwood (6:386) and repeated here:

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$$\dot{\psi} = I\dot{\gamma}_5/(I_0 - I)\cos\gamma_4 \tag{1}$$

where I is the target's moment of inertia about the \hat{n}_1 and \hat{n}_2 axes and I_0 is the target's moment of inertia about the spin axis, \hat{n}_3 .

The two rotational degrees of freedom required at the universal joint include rotation, γ_4 , about an axis \hat{g}_4 parallel to \hat{b}_1 and rotation γ_5 , about an axis g_5 parallel to g_5 . The rotational degrees of freedom for the momentum wheels labelled 1, 2, and 3 are axes \hat{g}_1 , \hat{g}_2 , and \hat{g}_3 respectively. These three axes are parallel to the corresponding \hat{b} frame axes, with the wheel joints themselves taken to be at the mass centers of the wheels. From this initial docked configuration the problem is to drive the system to a final spin-stabilized state with a set of feedba

controls. This final state is specified by requiring the joint location to coincide with the \hat{b}_3 axis, and that the cone angle, γ_4 , and spin rate $\dot{\gamma}_5$, be reduced to steady state values of zero.

In the following equations of motion, all vectors and scalar rates are with respect to the ê basis fixed in the main body, the OMV. The attitude equations for the OMV-target satellite system can be derived directly from the extended equations given by Conway and Widhalm (5) and are:

$$\begin{bmatrix} a_{00} & a_{01} & \cdots & a_{05} \\ a_{10} & a_{11} & \cdots & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & \\ & & & \\ & & \\ & & & \\$$

where

$$a_{00} = \sum_{\lambda} \sum_{\mu} \Phi_{\lambda\mu} , \text{ a dyadic}$$

$$a_{0k} = \sum_{\lambda} \sum_{\mu} \epsilon_{k\mu} \Phi_{\lambda\mu} . \hat{g}_{k} , \text{ a vector}$$

$$a_{i0} = \hat{g}_{i} . \sum_{\lambda} \sum_{\mu} \epsilon_{i\lambda} \Phi_{\lambda\mu} , \text{ a vector}$$

$$a_{ik} = \hat{g}_{i} . \sum_{\lambda} \sum_{\mu} \epsilon_{i\lambda} \epsilon_{k\mu} \Phi_{\lambda\mu} . \hat{g}_{k} , \text{ a scalar}$$
(3)

and $\epsilon_{i\mu}$ = $\begin{cases} 1, & \text{if } \hat{g_i} \text{ belongs to a joint anywhere on the chain} \\ & \text{of bodies connecting } \mu \text{ and the reference body (0)} \\ 0, & \text{otherwise (e.g. if } \mu = 0) \end{cases}$

and
$$\overline{G} = \overline{D}_{04}^{R} + 2\overline{\omega}_{0} \times \overline{D}_{04}^{R}$$
 (4)

$$\boldsymbol{\phi}_{\lambda\lambda} = \boldsymbol{\phi}_{\lambda} + m_{\lambda} \left[\bar{D}_{\lambda}^{2} 1 - \bar{D}_{\lambda} \bar{D}_{\lambda} \right] + \sum_{\mu \neq \lambda} m_{\mu} \left[\bar{D}_{\lambda\mu}^{2} 1 - \bar{D}_{\lambda\mu} \bar{D}_{\lambda\mu} \right]$$
 (5)

$$\Phi_{\lambda\mu} = -m[\bar{D}_{\mu\lambda}, \bar{D}_{\lambda\mu}] - \bar{D}_{\mu\lambda}\bar{D}_{\lambda\mu}]$$
 (6)

$$\overline{D}_{\lambda} = -\sum_{\mu \neq \lambda} m_{\mu} m^{-1} \overline{L}_{\lambda \mu}$$
 (7)

$$\bar{D}_{\lambda\mu} = \bar{D}_{\lambda} + \bar{L}_{\lambda\mu} \tag{8}$$

The vector $\bar{L}_{\lambda\mu}$ is the vector from the center of mass of body λ to the joint leading to body μ . $\bar{E}_{\lambda}^{\star}$ is determined from

$$\overline{E}_{\lambda}^{\star} = \overline{E}_{\lambda} - \sum_{\mu} \phi_{\lambda\mu}. \quad \sum_{k} \epsilon_{k\mu} \dot{\gamma}_{k} \quad \hat{g}_{k}$$
 (9)

and \vec{E}_{λ} is the vector

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$$\bar{E}_{\lambda} = 3Y\bar{\rho}^{-3} \hat{\rho} \times \phi_{\lambda\lambda}. \hat{\rho} - \bar{\omega}_{\lambda} \times \phi_{\lambda\lambda}. \bar{\omega}_{\lambda} + \bar{T}_{\lambda}^{'} + \sum_{j \in J_{\lambda}} \bar{T}_{\lambda j}^{SD}
+ \bar{D}_{\lambda} \times \bar{F}_{\lambda}^{'} + \sum_{\mu \neq \lambda} \bar{D}_{\lambda\mu} \times [\bar{F}_{\mu}^{'} + m\bar{\omega}_{\mu} \times (\bar{\omega}_{\mu} \times \bar{D}_{\mu\lambda})
+ m\bar{\rho}^{-3} (1 - 3\hat{\rho}\hat{\rho}) . \bar{D}_{\mu\lambda}]$$
(10)

In Eq (2) $\overline{\omega}_0 = \omega_{01} \hat{e}_1 + \omega_{02} \hat{e}_2 + \omega_{03} \hat{e}_3$, and the γ_i correspond to degrees of freedom about the unit vectors g_i . Superscript R implies that the indicated time differentiation is performed with respect to an observer fixed in the \hat{e} -frame. From Eqs (7) and (8) and from the definition given for $\overline{L}_{\lambda\mu}$, it is clear that the indicated time derivatives of \overline{D}_{04} are determined from the universal joint motion alone since the momentum wheel joints do not move with respect to the OMV. The joint motion is specified as are the control torques \overline{T}^{SD} in Eq (10). In this analysis, the external torques \overline{T}^i are the three orthogonal thruster torques acting on the OMV, and all external forces are assumed zero. In addition, all gravitational terms are ignored (all terms containing the position vector $\overline{\rho}$). The way in which the control torques (including

thruster torques) and the joint motion is specified is covered in the next chapter.

}

The constraint forces and torques have been eliminated from the equations of motion as described earlier. These quantities can be determined by the methods described in references (3) and (4). The expressions for the constraint force and torque at the universal joint are:

$$\vec{F}_{04}^{H} = (m - m_4) \vec{\tau}_{0}$$
 (11)

$$\bar{T}_{41}^{C} = (\Phi_{44} + \Phi_{40}) \cdot \dot{\omega}_{0} + (\Phi_{44} \cdot \hat{g}_{4}) \ddot{\gamma}_{4}
+ (\Phi_{44} \cdot \hat{g}_{5}) \ddot{\gamma}_{5} - \bar{E}_{4}^{*} - m\bar{D}_{40} \times \bar{G}$$
(12)

where \overline{r}_0 is the position vector of the mass center of the OMV-momentum wheel combination, relative to the system center of mass, and where \overline{G} is as given in Eq (4).

III. Nonlinear Feedback Control

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The detumbling and despinning problem presented here involves driving the universal joint connecting the OMV and target satellites across the face of the OMV to a point coincident with the \hat{b}_3 axis (see Fig. 2). Feedback control is used to maintain the attitude of the five-body system in such a way that the final state of the system is spin stabilized. The problem solution incorporates a feedback control approach in which an eight element control vector, $\bar{\mathbf{u}}$, is a nonlinear function of the system state variables. In this chapter the eight controls are defined so that the equations of motion can be written in a simpler form more suitable for Liapunov analysis. This procedure closely parallels that described by Widhalm and Conway (7:6-9) in their derivation of a control law for the two-body satellite system described earlier. Liapunov's direct method is then used to derive a control law which is globally asymptotically stable with respect to the spin-stabilized equilibrium state.

Eq (2) is first written in the form

$$A \dot{\bar{x}} = \bar{F}^* \tag{13}$$

where A is defined as the 8 x 8 matrix on the left-hand side of Eq (2). The vector, \overline{F}^* , is defined as the eight element vector on the right-hand side of Eq (2), and

$$\dot{\bar{x}} = [\dot{x}_{1} \dot{x}_{2} \dot{x}_{3} \dot{x}_{4} \dot{x}_{5} \dot{x}_{6} \dot{x}_{7} \dot{x}_{8}]^{T}$$

$$= [\dot{\omega}_{01} \dot{\omega}_{02} \dot{\omega}_{03} \ddot{\gamma}_{1} \ddot{\gamma}_{2} \ddot{\gamma}_{3} \ddot{\gamma}_{4} \ddot{\gamma}_{5}]$$
(14)

Eq (14) is derived from the state variables

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$$\bar{x} = [x_1 x_2 x_3 x_4 x_5 x_6 x_7 x_8]^{T}$$

$$= [\omega_{01} \omega_{02} \omega_{03} \dot{\gamma}_1 \dot{\gamma}_2 \dot{\gamma}_3 \dot{\gamma}_4 \dot{\gamma}_5]^{T}$$
(15)

The control vector, $\overline{\mathbf{u}}$, can be selected (7:6) so that Eq (13) can be written as

$$A \dot{\overline{x}} = \overline{F} + \overline{u} \tag{16}$$

Since the components of the vector, $\dot{\bar{x}}$, are the three angular acceleration components of the OMV, the three scalar angular accelerations of the othogonal momentum wheels, and the angular accelerations of the target about the two degrees of freedom at the joint, the appropriate control vector components are apparent. The control vector, \bar{u} , is composed of three orthogonal (thruster) torques about each of the \hat{e} -basis vectors, three internal torques applied at the wheel axes, and finally two internal torques applied in the two degrees of freedom of the universal joint. These control torques are designated u_1 through u_8 , respectively. Premultiplying Eq (16) by the inverse of matrix A yields

$$\dot{\bar{\mathbf{x}}} = \mathbf{A}^{-1} \, \bar{\mathbf{F}} + \mathbf{A}^{-1} \, \bar{\mathbf{u}} \tag{17}$$

since the matrix, A, will always be invertible for physical systems. The system of Eq (2) is augmented with the kinematical equation

$$\dot{x}_{Q} = x_{7} \tag{18}$$

where x_9 is defined as the target precession angle, γ_4 , and completes the set of equations of attitude motion. We define the augmented state

vector, $_{1}\overline{x}_{9}$, to contain the vector, \overline{x} , plus the ninth element, x_{9} .

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To derive the control vector, $\bar{\mathbf{u}}$, as a nonlinear function of the augmented state vector, $\mathbf{1}\overline{\mathbf{x}}_{\mathbf{q}}$, and the joint motion, a lemma presented by Vidyasagar (8) is applied. The lemma applies to autonomous systems, and the system of Eq (16) is nonautonomous because the OMV-target connecting joint motion is a specified function of time. Widhalm and Conway (7:7) have suggested that, by specifying the joint motion as a third order linear system which is asymptotically stable with respect to the desired final joint position, the third order system with Eqs (17) and (18) form an autonomous system. Since the desired final joint position relative to the \hat{b} -frame is given by the vector [0 0 c] , and since the HM equations are written in terms of the \hat{e} -frame, we define the vector, \tilde{c} , to be the vector leading from the origin of the b basis to the mass center of the OMV, the origin of the e-frame. The scalar values that are to be driven to zero for asymptotically stable joint motion are the position, velocity, and acceleration components of the joint lying along the b_2 axis. These scalars are given by:

$$(\bar{c} + \bar{L}_{04}) \cdot \hat{b}_2 = y_1$$

$$\dot{\bar{L}}_{04}^R \cdot \hat{b}_2 = y_2 = \dot{y}_1$$

$$\ddot{\bar{L}}_{04}^R \cdot \hat{b}_2 = y_3 = \dot{y}_2$$
(19)

The derivative of the vector, \overline{c} , does not appear since the vector position of the OMV mass center relative to the geometric center of the OMV is constant. The complete autonomous system required for the application of the previously mentioned lemma is given by Eqs (17), (18), and (19)

and is formed by writing

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$$\dot{\bar{x}} = A^{-1} \bar{F} + A^{-1} \bar{u}$$

$$\dot{x}_9 = x_7$$

$$\dot{\bar{y}} = D \bar{y}$$
(20)

where D is a negative definite matrix selected to obtain the desired decay of the scalar y_1 given in Eq (19). The joint motion terms contained in the matrix, A, and in the vector, \overline{F} , are now specified by the vector \overline{y} leaving the system, (20), independent of time.

The lemma developed by Vidyasagar (8:157) in his discussion of Liapunov's direct method now applies to the system, (20), and is stated as follows: "Let $V(_1x_9, y)$ be continuously differentiable and suppose that for some $d \ge 0$ the set

$$S_d^* = [\overline{x}_9, \overline{y} : V(\overline{x}_9, \overline{y}) \leq d]$$

is bounded. Suppose that V is bounded below over the set S_d^* and that $\dot{V}(_1\overline{x}_9, \overline{y}) \leq 0$ for all $_1\overline{x}_9$ and \overline{y} in S_d^* . Let S denote the subset of S_d^* defined by

$$S = [\overline{x_9}, \overline{y} \quad S_d^* : \dot{V}(\overline{x_9}, \overline{y}) = 0]$$

and let M be the largest invariant set of a system which is contained in S. Then whenever $1^{\overline{X}_9}(0)$ and $\overline{y}(0)$ are members of S_d^* , the solution of the system, (20), approaches M as $t \to \infty$."

Now M is an invariant set of system, (20), if every trajectory starting from an initial point in M remains in M for all time. Since the system, (20), is autonomous every trajectory through its state space is

an invariant set (8:156). The task then is to find a candidate Liapunov function, V, that meets the requirements of the lemma. To derive a non-linear feedback control law that drives the five-body system to the desired final state of spin-stabilized equilibrium, Widhalm and Conway (7) suggested a candidate Liapunov function like

$$V = (1/2) \bar{x}^T I \bar{x} + (1/2) K x_9^2 + \bar{y}^T R \bar{y}$$
 (21)

where I is the identity matrix, K is a positive constant, and R is a positive definite constant matrix. The function is continuously differentiable, and it is easy to select a vector $1^{\overline{\chi}}_9$ and a constant, d, to demonstrate that a set like S_d^* exists.

The condition on $\mathring{V}(\sqrt{x_9}, \overline{y})$ must be satisfied; differentiating V with respect to time yields

$$\dot{V} = \overline{X}^{T} I \dot{\overline{X}} + K \times_{Q} \dot{X}_{Q} + \dot{\overline{y}}^{T} R \overline{y} + \overline{y}^{T} R \dot{\overline{y}}$$
 (22)

Substitution from the system, (20), gives the result

$$\dot{V} = \overline{X}^{T} I \left[A^{-1} \overline{F} + A^{-1} \overline{u} \right] + K \times_{9} \times_{7}$$

$$+ \overline{y}^{T} \left[D^{T} R + R D \right] \overline{y}$$
(23)

Now since R is a positive definite matrix and D was specified to be a negative definite matrix, then the expression $D^\mathsf{T}R + RD$ is negative definite. Writing the Liapunov matrix equation

$$-Q = D^{\mathsf{T}} R + R D \tag{24}$$

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$$\mathbf{\tilde{V}}^{\star} = -\mathbf{\overline{y}}^{\mathsf{T}} \mathbf{Q} \mathbf{\overline{y}}^{\mathsf{T}} \tag{25}$$

implies both that Q is positive definite from Eq (24) and that as a result both V^* and $-\dot{V}^*$ are positive definite (8:172). Thus the third term in Eq (23) is negative definite. To make \dot{V} at least negative semi-definite, select the control vector

$$\vec{u} = -\vec{F} + A \begin{bmatrix} 0 & 0 & 0 & 0 & 0 & -Kx_9 & 0 \end{bmatrix}^T - A B \vec{x}$$
 (26)

where the matrix B is positive definite or positive semi-definite. If the matrix B is positive definite, then V is negative semi-definite in x_g . However, if the elements of B are positive except for $B_{33}=0$, V is negative semi-definite in x_3 and x_g . Then from the above lemma the system, (20), with control vector \vec{u} of Eq (26) is asymptotically stable with respect to the largest invariant set contained in the x_3 , x_g plane. But from Eq (26) it can be seen that any non-zero x_g results in a non-zero control vector \vec{u} , which in turn causes a departure from the x_3 , x_g plane. Therefore the largest invariant set lies in the x_3 , x_g plane, but only in that region where x_g is zero, namely the x_3 axis. The control vector \vec{u} of Eq (26) is then the desired nonlinear feedback control law for spin-stabilization of this system.

Non-zero off-diagonal terms must be included in the B matrix of Eq (26) which will couple the momentum wheel torques to state variables other than just the momentum wheel angular velocities. The torques must be coupled to the state variables in such a way that the angular rates of the \hat{g}_1 and \hat{g}_2 wheels decay to zero, so that the system stabilizes in pure spin. Implementing the control law of Eq (26) requires the determination of the non-zero elements of the matrix B, and the constant K. In their work with the two-body satellite system, Widhalm and Conway have suggested

that controls can be kept within reasonable limits by ensuring that the target center of mass does not depart appreciably from the \hat{b}_3 axis. This can be accomplished by selection of the matrix D, which controls the universal joint motion, in conjunction with K and the B₇₇ element of the B matrix. Joint motion can be specified which will closely follow the decay of the target's precession angle, and maintain the proximity of the target mass center to the b_3 spin axis. Finally, substitution of the control vector \bar{u} of Eq (26) into Eq (20) yields the complete, linear system

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$$\dot{\bar{x}} = [0 \ 0 \ 0 \ 0 \ 0 \ -Kx_{9} \ 0]^{T} - B \bar{x}$$

$$\dot{x}_{9} = x_{7}$$

$$\dot{\bar{y}} = D \bar{y}$$
(27)

From Eq (27) it can be clearly seen that if the matrix B is diagonal, and if the initial momentum wheel angular rates as well as the OMV angular velocity components ω_{01} and ω_{02} are zero, they will remain zero throughout the detumbling process. In the case where the only off-diagonal terms in B are those coupling the momentum wheel torques to selected system states, the ω_{01} and ω_{02} angular velocity components of the OMV still remain zero. This implies that the throughout the maneuver the OMV remains in a state of pure spin.

IV. Results

In this chapter the basis for the selection of initial conditions and system mass properties is presented, as well as the values selected. System state histories and control torque histories are presented for four detumbling maneuvers. The four maneuvers include detumbling with feedback control without momentum wheel coupling, feedback control with a single momentum wheel coupled, detumbling using only gimbal (joint) torques, and finally, detumbling using only gimbal torques for the first 250 seconds, followed by 50 seconds of feedback control applying the full control torque vector with one wheel coupled. Representative histories for the constraint loads at the joint between the OMV and the target satellite are also given.

System mass properties were selected based on values used in previous research (9). The mass properties of the composite body consisting of the OMV and the three attached momentum wheels were selected to duplicate those of the OMV model used by Widhalm (9). Reasonable but arbitrary values of mass and moments of inertia were then selected for the three identical wheels. From this information and by specifying the location of the mass center of the composite OMV-momentum wheel system, the mass and inertia matrix for the OMV (without wheels) were computed. In this way direct comparisons could be made between the two-body and five-body analyses by completely decoupling the wheel control torques from all non-zero system states. As mentioned previously, this is accomplished by selecting all off-diagonal terms of the matrix B in the linear system (27) to be zero. Under this condition, the values of elements B_{44} , B_{55} , and B_{66} are completely arbitrary. In addition to the various mass

properties, the system state variable initial conditions were also duplicated from reference (9). The mass properties and initial conditions are given in Tables I and II, respectively.

From Eq (27) and from the discussion that immediately follows it, it can be seen that the values selected for elements B_{11} and B_{22} are also arbitrary, since they will always be multiplied by states \mathbf{x}_1 and \mathbf{x}_2 , which remain equal to zero throughout the detumbling, despinning maneuver. The values actually selected are those used by Widhalm (9) in the application of feedback control to the two-body satellite system. In that case states \mathbf{x}_1 and \mathbf{x}_2 attained non-zero values after approximately 290 seconds of open-loop control. Feedback control was then applied in an attempt to spin-stabilize the system, the desired response being obtained using the values $B_{11} = B_{22} = 0.046$.

The remaining constants to be determined include B_{77} , B_{88} , K, and the elements of the D matrix of the third order joint motion equation in Eq (27). Selecting the scalar equation from the 12 equation system of Eq (27) corresponding to the target precession angle motion, the constants B_{77} and K can be determined by specifying a desired final precession angle at the end of the maneuver. A total maneuver time of 300 seconds was selected, and critical damping specified. A final precession angle corresponding to the target mass center on the OMV spin axis and a final joint position equal to 0.05% of initial joint position was specified. The result obtained from these requirements is a solution with equal eigenvalues of about -0.035, with $B_{77} = 0.07$ and K = 0.00123. In a similar way, with the specification of the final joint position just given and with critical damping of the joint motion, equal eigenvalues

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TABLE I

Satellite Mass Properties

| | MASS | ¹ 1 | ^I 2 | ^I 3 |
|------------------|---------|------------------------|------------------------|-------------------------|
| Target Satellite | 1000 Kg | 1000 Kg-m ² | 1000 Kg-m ² | 1100 Kg-m ² |
| OMV | 4500 Kg | 6400 Kg-m ² | 6400 Kg-m ² | 11800 Kg-m ² |
| Momentum Wheels | 10 Kg | 25 Kg-m ² | 25 Kg-m ² | 55 Kg-m ² |

TABLE II

Initial Conditions

| Variable | Meaning | Value |
|---|---|-------|
| ω_{01} | ê _l component OMV angular velocity | 0.0 |
| ω ₀₂ | ê ₂ component OMV angular velocity | 0.0 |
| ω_{03} | $\hat{\mathbf{e}}_3$ component OMV angular velocity | 0.102 |
| Ϋ́ ₁ | #1 momentum wheel spin rate | 0.0 |
| | #2 momentum wheel spin rate | 0.0 |
| ν̈ ₂ ν˙ ₃ ν˙ ₄ | #3 momentum wheel spin rate | 0.0 |
| $\dot{\gamma}_{f 4}$ | target precession angle rate | 0.0 |
| $\dot{\gamma}_{5}$ | target spin rate | 0.009 |
| $(\overline{L}_{04} + \overline{c}) \cdot \hat{b}_2$ | joint position | 0.599 |
| τ̈ ₀₄ · β̂ ₂ | joint velocity | 0.0 |
| Ë ₀₄ · β̂ ₂ | joint acceleration | 0.0 |
| γ ₄ | target precession angle | 0.349 |

Note: Values in TABLE II are given in meters, radians, or radians per second, as applicable.

of -0.04 were obtained for the joint motion equation. This resulted in values of D_{31} = -0.000064, D_{32} = -0.0048, and D_{33} = -0.12. Finally, solving the eighth scalar equation of the system of Eq (27) by requiring that the target spin rate be reduced to 0.5% of its initial value yields the value of B_{98} = 0.02.

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With the momentum wheels uncoupled the system behavior was identical to that of the two-body system in Fig. 1, verified by the comparison of the results with those of Widhalm (9). Wheel torques were zero, with the OMV thrust torques and universal joint torques given in Figs. 3 and 4. None of these control torques reached large values, and it can be seen that the controls vary smoothly with time with no abrupt changes. The joint motion and precession angle decay behaved as specified, decaying to the small final values specified with no overshoot. The results are given in Fig. 5. The target spin rate decay displayed similar behavior. The precession angle rate of change and target spin rate histories are given in Fig. 6, where it can be seen that no radical motion has occurred. The constraint loads at the universal joint due to lack of rotational freedom and due to the loading required to drive the joint across the OMV were relatively small. The constraint torque maximum value was approximately 2 Nm, and the maximum force encountered in driving the joint was about 1 N. These results are shown in Fig. 7, where the magnitude of the constraint force is plotted, as well as the component of that force lying along the axis of joint motion. This b, component corresponds to the load capacity that would be required for a jackscrew, for instance, were such a device used on the OMV to obtain the desired joint motion.

Although global asymptotic stability is only guaranteed by the

lemma used earlier for the case of feedback control with the control law of Eq (26), it was of interest to attempt system despin and detumbling using only control torques applied at the universal joint. The result was that the system displayed no radical or unusual behavior, and approached a nearly spin-stabilized state after 300 seconds of control. The OMV still remained in a state closely approximating pure spin, although non-zero angular velocity components did remain. Figs. 8 and 9 show the OMV angular velocity history for this maneuver, and indicate that the departure from pure spin was modest. Constraint torque and interaction force at the connection also remained small, although as indicated in Figs. 10 and 11, a quasi-steady state condition was reached with continuous constraint and control torques experienced at the joint. A residual precession angle remained after the maneuver, but the rate of change of the precession angle was very small, indicating that the available control torques were able to maintain the system configuration but unable to change it at any appreciable rate. Although there was some oscillation in the precession angle rate of change, no other violent behavior occured with respect to either target spin or precession angle changes. The results are shown in Figs. 12 and 13.

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The maneuver described above was repeated, but at 250 seconds the full control vector was applied in an attempt to spin-stabilize the system. The residual non-zero ω_{02} component of the OMV angular velocity was reduced nearly to zero, and the OMV spin rate brought to a steady value (see Figs. 14 and 15). The relative spin rate of the target and the precession angle rate of change were likewise reduced to very nearly zero as indicated in Fig. 16. Although not plotted, the precession angle of

the target was reduced to half of its value at 250 seconds, or approximately 0.9 degrees. Figs. 17 through 19 show the attendant reductions in the constraint and control torques and in the constraint force at the joint. These data clearly indicate that the system is moving toward a spin stabilized equilibrium.

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An attempt was made to couple the momentum wheels to the target precession angle rate and spin rate. The magnitude of the OMV thruster torque about each of the \hat{b} axes was integrated over the maneuver period, and the three resulting values added to obtain some measure of the total torque power required from the thrusters. The resulting total was then compared for maneuvers completed using various off-diagonal gain terms in the B matrix of Eq (26). No attempt at using control torque on the \hat{b}_3 wheel yielded a reduction in the OMV thruster torque requirements. Using applied torque at the \hat{b}_2 wheel by setting B_{57} to 1.0 resulted in a reduction of the integrated thrust torque from 436 Nm-sec for no wheel coupling to approximately 377 Nm-sec. The resulting thruster control torques and momentum wheel control torque are shown in Figs. 20 and 21. Fig. 21 also includes the \hat{b}_2 momentum wheel angular rate history during the maneuver.

These results indicate that the system is well behaved in the sense that despinning and detumbling can be accomplished with relatively small control requirements, and that no violent dynamical behavior occurs even when internal control torques only are applied. Also, the use of momentum wheels to reduce thruster requirements is possible, although no evidence is presented that the wheels provide any major benefit in terms of efficient system control.

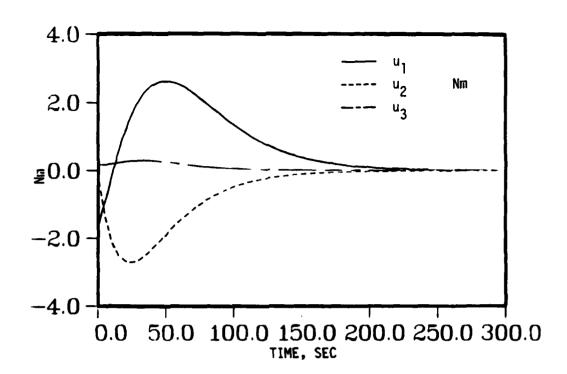


Fig. 3. OMV Thrust Torques, Momentum Wheels Uncoupled.

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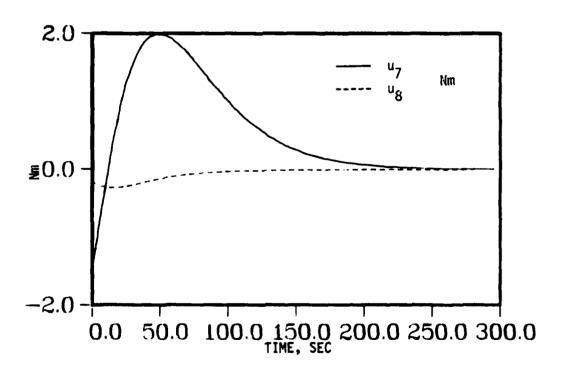


Fig. 4. Gimbal (Universal Joint) Torques, Uncoupled Momentum Wheels.

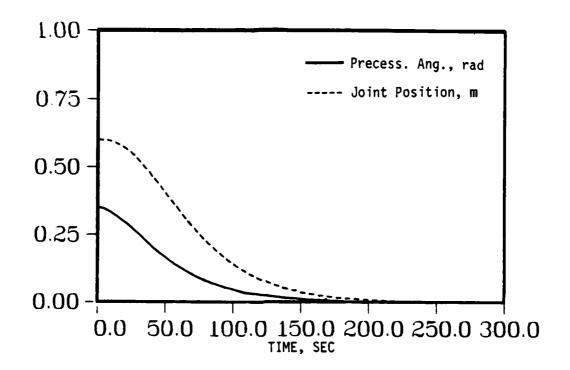


Fig. 5. Joint Position and Precession Angle Decay

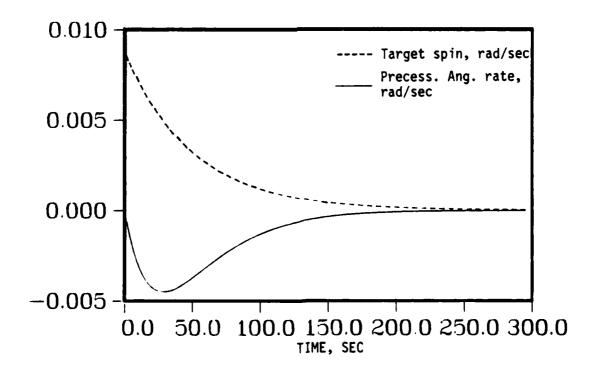


Fig. 6. Target Spin and Precession Rate Decays

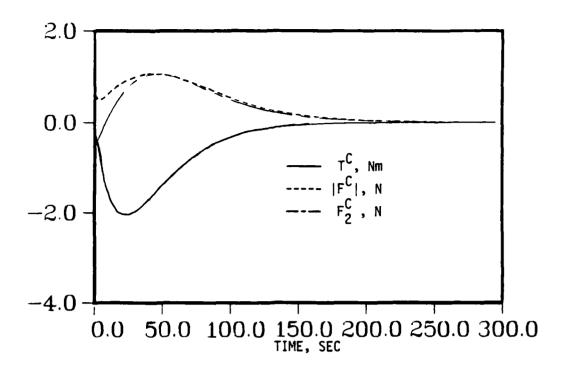
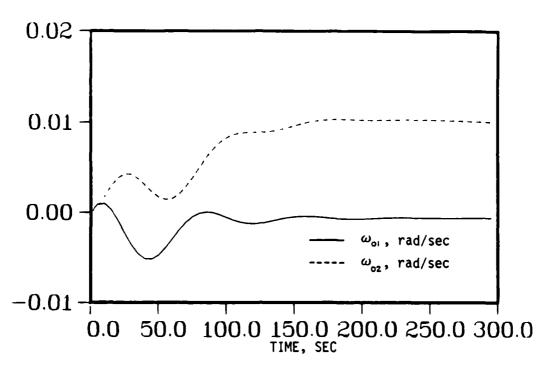


Fig. 7. Constraint Loads at Universal Joint

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Fig. 8. Angular Velocities of OMV with u_7 and u_8 Feedback Only

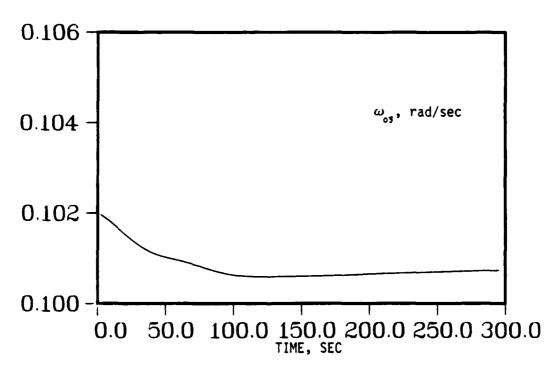
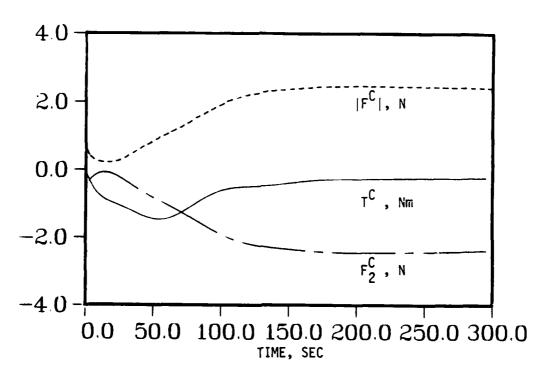


Fig. 9. Angular Velocity $\omega_{\rm o3}$ of OMV with $\rm u_7$ and $\rm u_8$ Feedback Only



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Fig. 10. Joint Constraint Loads, u_7 and u_8 Feedback Only

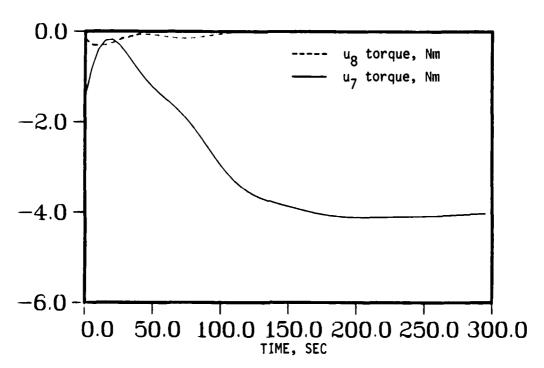
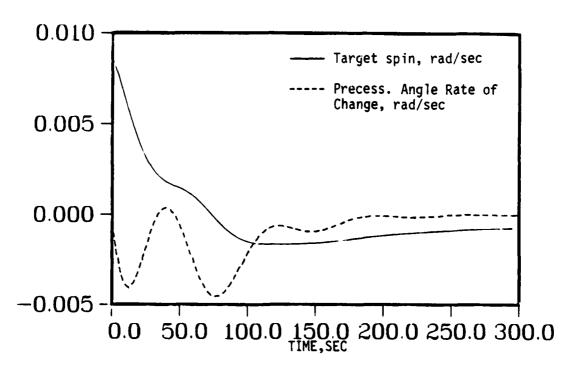


Fig. 11. Control Torque History, u_7 and u_8 Feedback Only



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Fig. 12. Target Spin and Precession Angle Rates, u₇ and u₈ Feedback Only

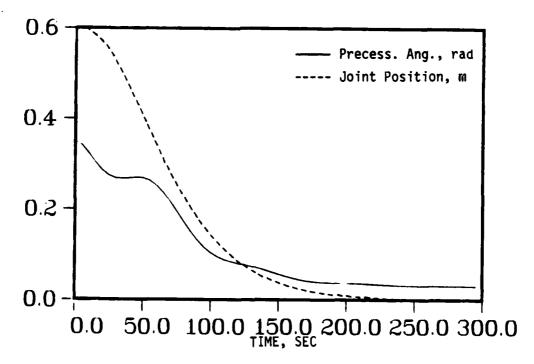


Fig. 13. Target Precession Angle and Joint Position, u_7 and u_8 Feedback Only

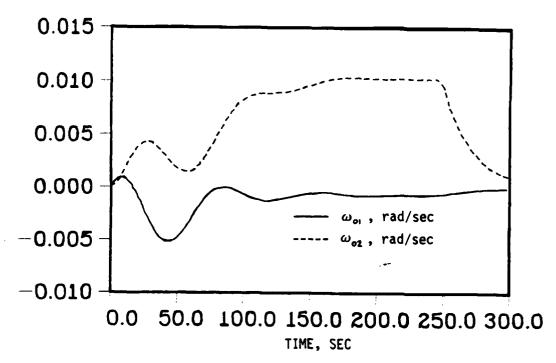


Fig. 14. OMV Angular Velocity Components; Full Feedback Added at t = 250 seconds

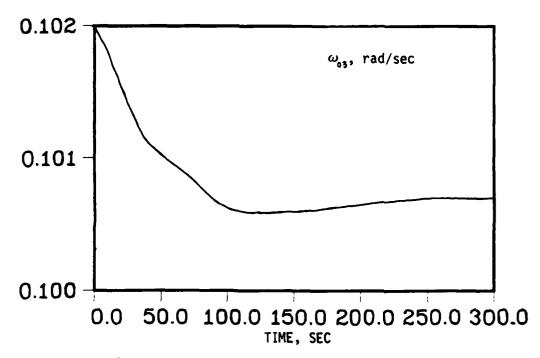
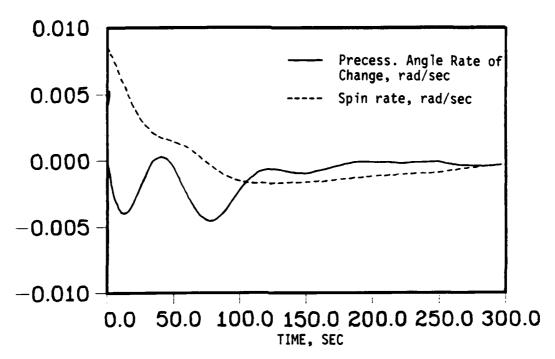


Fig. 15. OMV \hat{b}_3 Angular Velocity Component; Full Feedback Added at $t^3 = 250$ seconds



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Fig. 16. Precession Angle Rate of Change and Target Spin Rate; Full Feedback Added at t = 250 seconds

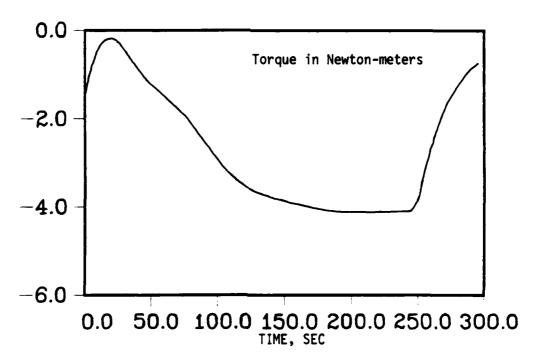
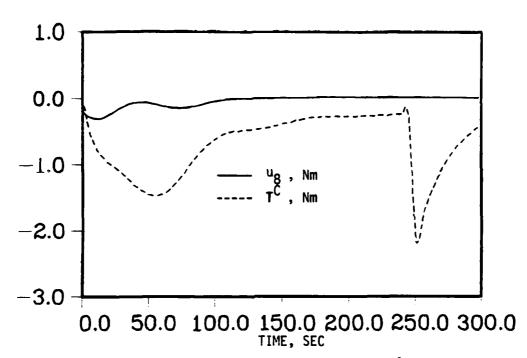


Fig. 17. Gimbal Control Torque u_7 With Full Feedback Added at t=250 seconds



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Fig. 18. Control Torque u_8 and Constraint Torque T^C ; Full Feedback at t=250 seconds

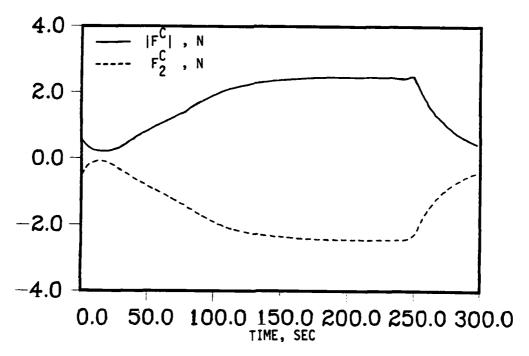


Fig. 19. Constraint Force Magnitude and 6, Component; Full Feedback Added at t = 250 seconds

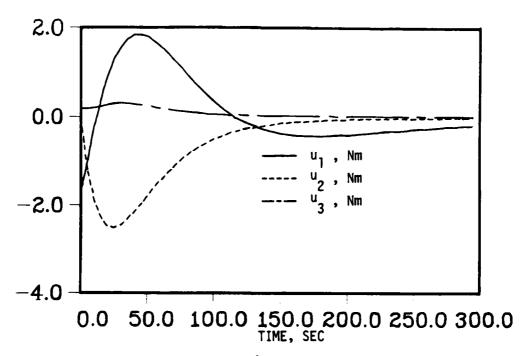


Fig. 20. OMV Thruster Torques, b. Momentum Wheel Torque Coupled to Target Precession Angle

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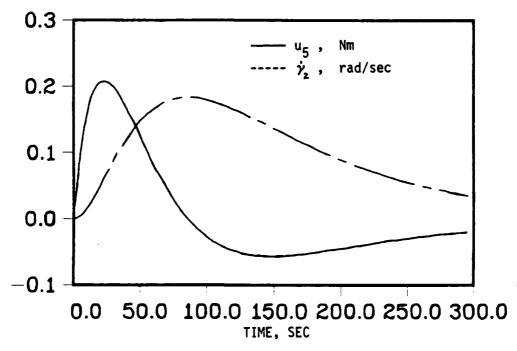


Fig. 21. \hat{b}_2 Momentum Wheel Control Torque, u_5 , and Wheel Angular Vel.; Control Torque u_5 Coupled to Precession Angle

| 0 -1.500192 .000 .613576 5822242984 .503225 10176267 -1.576 .631 .097 15 .399274 -1.897 .759 .374 20 .884267 -2.032 .839 .601 25 1.273251 -2.043 .935 .778 30 1.568230 -1.973 .993 .907 35 1.777207 -1.853 1.033 .992 40 1.909183 -1.705 1.056 1.041 45 1.976161 -1.545 1.061 1.058 50 1.989140 -1.382 1.051 1.055 55 1.959121 -1.224 1.027 1.023 60 1.895104 -1.076 .990 .981 65 1.808090939 .945 .928 70 1.703077815 .892 .869 75 1.588067704 .835 .806 80 1.468058606 .775 .741 85 1.346050520 .714 .676 85 1.399033324 .538 .496 100 .998033324 .538 .496 100 .998033324 .538 .496 100 .998033324 .538 .496 100 .998033324 .538 .496 100 .998033324 .538 .496 100 .998033324 .538 .496 100 .998033324 .538 .496 100 .998033324 .538 .496 100 .998033324 .538 .496 100 .998033324 .538 .496 100 .998033324 .538 .496 105 .894029276 .488 .433 110 .797025235 .434 .393 115 .708022200 .387 .348 120 .626020170 .344 .307 125 .552018144 .304 .270 140 .371012089 .207 .180 140 .371012089 .207 .180 140 .371012089 .207 .180 140 .371012089 .207 .180 155 .182007040 .103 .087 175 .135 .004014 .009 .055 .137 .117 160 .281010064 .157 .136 150 .281010064 .157 .136 150 .281010064 .157 .136 150 .281010064 .157 .136 150 .281010064 .027 .077 .064 180 .116005025 .066 .055 185 .100005 .025 .066 .055 185 .100005 .025 .006 .057 180 .101 .005 .025 .006 .057 180 .101 .005 .002 .007 .004 190 .085 .004 .009 .005 .002 .007 190 .085 .004 .009 .005 .002 .007 190 .085 .004 .009 .005 .002 .007 190 .085 .004 .009 .005 .002 .007 190 .085 .004 .009 .005 .002 .007 190 .085 .004 .009 .005 .002 .007 190 .085 .004 .009 .005 .002 .007 190 .085 .004 .009 .005 .002 .007 190 .085 .004 .009 .002 .008 101 .005 .009 .002 .008 101 .005 .008 .009 .009 .002 .008 101 .005 .008 .009 .009 .002 .008 | time | u ₇ | u ₈ | TC | F ^C | F ^C ₂ |
|--|------|----------------|----------------|--------|----------------|-----------------------------|
| 5 822 242 984 .503 225 10 176 267 -1.576 .631 .097 15 .399 274 -1.897 .759 .374 20 .884 267 -2.032 .859 .601 25 1.273 251 -2.043 .935 .778 30 1.568 230 -1.973 .993 .707 35 1.777 207 -1.853 1.033 .992 40 1.909 183 -1.705 1.056 1.041 45 1.976 161 -1.545 1.061 1.058 50 1.989 140 -1.382 1.051 1.058 50 1.989 104 -1.076 .990 .981 65 1.808 090 939 .945 .928 70 1.703 077 815 .892 .869 75 1.588 | 0 | -1.500 | = | •000 | .613 | |
| 10 176 267 -1.576 .631 .097 15 .399 274 -1.897 .759 .374 20 .884 267 -2.032 .859 .601 25 1.273 251 -2.043 .935 .778 30 1.568 230 -1.973 .993 .907 35 1.777 207 -1.853 1.033 .992 40 1.909 183 -1.705 1.056 1.041 45 1.976 161 -1.545 1.061 1.058 50 1.989 140 -1.382 1.051 1.050 55 1.959 121 -1.224 1.027 1.023 60 1.895 104 -1.074 .990 .981 65 1.959 121 -1.224 1.027 1.023 70 1.703 077 815 .892 .869 75 1.588< | | | | | | |
| 15 .399 274 -1.897 .759 .374 20 .884 267 -2.032 .859 .601 25 1.273 251 -2.043 .935 .778 30 1.568 230 -1.973 .993 .907 35 1.777 207 -1.853 1.033 .992 40 1.909 183 -1.056 1.041 1.056 1.041 1.056 1.041 1.056 1.041 1.056 1.041 1.056 1.041 1.056 1.051 1.050 1.050 1.041 1.056 1.041 1.056 1.041 1.056 1.041 1.056 1.041 1.056 1.041 1.056 1.041 1.056 1.041 1.056 1.041 1.056 1.041 1.056 1.041 1.056 1.041 1.056 1.041 1.056 1.041 1.056 1.041 1.056 1.041 1.056 1.041 1.056 1.041 1.056 | | | | | | |
| 20 .884 267 -2.032 .8859 .601 25 1.273 251 -2.043 .935 .778 30 1.568 230 -1.973 .993 .907 35 1.777 207 -1.853 1.033 .992 40 1.909 183 -1.705 1.056 1.041 45 1.976 161 -1.545 1.061 1.058 50 1.989 140 -1.382 1.051 1.050 55 1.979 121 -1.224 1.027 1.023 60 1.895 104 -1.076 .990 .981 65 1.808 090 939 .945 .928 70 1.703 077 815 .892 .869 75 1.588 067 704 .835 .806 80 1.468 058 606 .775 .741 85 1.346 053 520 .714 .676 80 1.946 <t< td=""><td></td><td></td><td></td><td></td><td></td><td></td></t<> | | | | | | |
| 25 1.273 -2.251 -2.043 .935 .778 30 1.568 -2.30 -1.973 .993 .997 35 1.777 -2.07 -1.853 1.033 .992 40 1.909 -1.83 -1.705 1.056 1.041 45 1.976 -1.161 -1.545 1.061 1.058 50 1.989 -1.40 -1.382 1.051 1.055 50 1.989 -1.04 -1.076 .990 .981 60 1.895 -1.04 -1.076 .990 .981 65 1.808 -0.090 -939 .945 .928 70 1.703 -0.77 -815 .892 .869 75 1.588 -0.067 704 .835 .806 80 1.468 -0.058 606 .775 .741 85 1.346 -0.050 520 .714 .676 90 1.226 <td></td> <td></td> <td></td> <td></td> <td></td> <td></td> | | | | | | |
| 35 1.777 207 -1.853 1.033 .992 40 1.909 183 -1.705 1.056 1.041 45 1.976 161 -1.545 1.061 1.050 50 1.989 140 -1.382 1.051 1.050 55 1.959 121 -1.224 1.027 1.023 60 1.895 104 -1.076 .990 .981 65 1.808 090 939 .945 .928 70 1.703 077 815 .892 .869 75 1.588 067 704 .835 .806 80 1.468 058 606 .775 .741 85 1.346 059 520 .714 .676 90 1.226 043 445 .654 .613 95 1.109 038 380 .595 .553 100 .998 | 25 | 1.273 | 251 | | • 935 | .778 |
| 40 1.909 183 -1.705 1.056 1.041 45 1.976 161 -1.545 1.061 1.050 50 1.989 140 -1.382 1.051 1.050 55 1.959 121 -1.224 1.027 1.023 60 1.895 104 -1.076 .990 .981 65 1.808 090 939 .945 .928 70 1.703 077 815 .892 .869 75 1.588 067 704 .835 .806 80 1.468 058 606 .775 .741 85 1.346 058 606 .775 .741 90 1.226 043 445 .654 .613 95 1.109 038 380 .595 .553 100 .998 033 324 .538 .496 105 .894 029 276 .484 .443 110 .797 0 | 30 | 1.568 | 230 | -1.973 | .993 | .907 |
| 45 1.976 161 -1.545 1.051 1.058 50 1.989 140 -1.382 1.051 1.050 55 1.959 121 -1.224 1.027 1.023 60 1.895 104 -1.076 .990 .981 65 1.808 090 939 .945 .928 70 1.703 077 815 .892 .869 75 1.588 067 704 .835 .806 80 1.468 058 606 .775 .741 .676 85 1.346 050 520 .714 .676 90 1.226 043 445 .654 .613 95 1.109 038 380 .595 .553 100 .998 033 324 .538 .496 105 .894 029 276 .484 .443 .4393 | | | -,207 | -1.853 | 1.033 | .992 |
| 50 1.989 140 -1.382 1.051 1.050 55 1.959 121 -1.224 1.027 1.023 60 1.895 104 -1.076 .990 .981 65 1.808 090 939 .945 .928 70 1.703 077 815 .892 .869 75 1.588 067 704 .835 .806 80 1.468 058 606 .775 .741 85 1.346 050 520 .714 .676 90 1.226 043 445 .654 .613 95 1.109 038 380 .595 .553 100 .978 033 324 .538 .496 105 .894 029 276 .484 .443 110 .797 025 235 .434 .393 115 .708 < | | | | -1.705 | 1.056 | 1.041 |
| 55 1,959 -,121 -1,024 1,027 1,023 60 1,895 -,104 -1,076 .990 .981 65 1,808 -,090 -,939 .945 .928 70 1,703 -,077 -,815 .892 .869 75 1,588 -,067 -,704 .835 .806 80 1,468 -,058 -,606 .775 .741 85 1,346 -,050 -,520 .714 .676 90 1,226 -,043 -,445 .654 .613 95 1,109 -,038 -,380 .595 .553 100 .998 -,033 -,324 .538 .496 105 .894 -,029 -,276 .484 .443 110 .797 -,025 -,235 .434 .393 115 .708 -,022 -,200 .387 .348 120 .626 | | | | -1.545 | 1.061 | 1.058 |
| 60 1.895 104 -1.076 .990 .981 65 1.808 090 9339 .945 .928 70 1.703 077 815 .892 .869 75 1.588 067 704 .835 .806 80 1.468 058 606 .775 .741 85 1.346 050 520 .714 .676 90 1.226 043 445 .654 .613 95 1.109 038 380 .595 .553 100 .978 033 324 .538 .496 105 .894 029 276 .484 .443 110 .777 025 235 .434 .393 115 .708 022 200 .387 .348 120 .626 020 170 .344 .307 125 .552 | | | | | | |
| 65 1.808 090 939 .945 .928 70 1.703 077 815 .892 .869 75 1.588 067 704 .835 .806 80 1.468 058 606 .775 .741 85 1.346 050 520 .714 .676 90 1.226 043 445 .654 .613 95 1.109 038 380 .595 .553 100 .998 033 324 .538 .496 105 .894 029 276 .484 .443 110 .797 025 235 .434 .393 115 .708 022 200 .387 .348 120 .626 020 170 .344 .307 125 .552 018 144 .304 .270 130 .485 01 | | | | | | 1.023 |
| 70 1.703 077 815 .892 .869 75 1.588 067 704 .835 .806 80 1.468 058 606 .775 .741 85 1.346 050 520 .714 .676 90 1.226 043 445 .654 .613 95 1.109 038 380 .595 .553 100 .998 033 324 .538 .496 105 .894 029 276 .484 .443 110 .797 025 235 .434 .393 115 .708 022 200 .387 .348 120 .626 020 170 .344 .307 125 .552 018 144 .304 .270 130 .485 016 123 .268 .236 135 .425 01 | | | | | | |
| 75 1.588 067 704 .835 .806 80 1.468 058 606 .775 .741 85 1.346 050 520 .714 .676 90 1.226 043 445 .654 .613 95 1.109 038 380 .595 .553 100 .978 033 324 .538 .496 105 .894 029 276 .484 .443 110 .777 025 235 .434 .393 115 .708 022 200 .387 .348 120 .626 020 170 .344 .307 125 .5552 018 144 .304 .270 130 .4855 016 123 .268 .236 135 .425 014 104 .236 .207 140 .371 | | | | | | |
| 80 1.468 058 606 .775 .741 85 1.346 050 520 .714 .676 90 1.226 043 445 .654 .613 95 1.109 038 380 .595 .553 100 .978 033 324 .538 .496 105 .894 029 276 .484 .443 110 .777 025 235 .434 .393 115 .708 022 200 .387 .348 120 .626 020 170 .344 .307 125 .552 018 144 .304 .270 130 .485 016 123 .268 .236 135 .425 014 104 .236 .207 140 .371 012 089 .207 .180 145 .323 011 064 .157 .136 150 .281 010 | | | | | | |
| 85 1.346 050 520 .714 .676 90 1.226 043 445 .654 .613 95 1.109 038 380 .595 .553 100 .998 033 324 .538 .496 105 .894 029 276 .484 .443 110 .797 025 235 .434 .393 115 .708 022 200 .387 .348 120 .626 020 170 .344 .307 125 .552 018 144 .304 .270 130 .485 016 123 .268 .236 135 .425 014 104 .236 .207 140 .371 012 089 .207 .180 145 .323 011 076 .181 .156 150 .281 010 064 .157 .136 155 .244 009 | | | | | | |
| 90 1.226 043 445 .654 .613 95 1.109 038 380 .595 .553 100 .998 033 324 .538 .496 105 .894 029 276 .484 .443 110 .797 025 235 .434 .393 115 .708 022 200 .387 .348 120 .626 020 170 .344 .307 125 .552 018 144 .304 .270 130 .485 016 123 .268 .236 135 .425 014 104 .236 .207 140 .371 012 089 .207 .180 145 .323 011 064 .157 .136 150 .281 010 064 .157 .136 155 .244 009 055 .137 .117 160 .211 008 | | | | | | |
| 95 1.109 038 380 .595 .553 100 .998 033 324 .538 .496 105 .894 029 276 .484 .443 110 .797 025 235 .434 .393 115 .708 022 200 .387 .348 120 .626 020 170 .344 .307 125 .552 018 144 .304 .270 130 .485 016 123 .268 .236 135 .425 014 104 .236 .207 140 .371 012 089 .207 .180 145 .323 011 069 .207 .180 145 .323 011 064 .157 .136 150 .281 010 064 .157 .136 155 .244 009 055 .137 .117 160 .211 008 | | | | | | |
| 100 .998 033 324 .538 .496 105 .894 029 276 .484 .443 110 .797 025 235 .434 .393 115 .708 022 200 .387 .348 120 .626 020 170 .344 .307 125 .552 018 144 .304 .270 130 .485 016 123 .268 .236 135 .425 014 104 .236 .207 140 .371 012 089 .207 .180 145 .323 011 076 .181 .156 150 .281 010 064 .157 .136 155 .244 009 055 .137 .117 160 .211 008 047 .119 .101 165 .182 007 040 .103 .087 170 .157 007 | | | | | | |
| 105 .894 029 276 .484 .443 110 .797 025 235 .434 .393 115 .708 022 200 .387 .348 120 .626 020 170 .344 .307 125 .552 018 144 .304 .270 130 .485 016 123 .268 .236 135 .425 014 104 .236 .207 140 .371 012 089 .207 .180 145 .323 011 076 .181 .156 150 .281 010 064 .157 .136 155 .244 009 055 .137 .117 160 .211 008 047 .119 .101 165 .182 007 040 .103 .087 175 .135 007 034 .089 .075 175 .135 006 | | | | | | |
| 110 .797 025 235 .434 .393 115 .708 022 200 .387 .348 120 .626 020 170 .344 .307 125 .552 018 144 .304 .270 130 .485 016 123 .268 .236 135 .425 014 104 .236 .207 140 .371 012 089 .207 .180 145 .323 011 076 .181 .156 150 .281 010 064 .157 .136 155 .244 009 055 .137 .117 160 .211 008 047 .119 .101 165 .182 007 040 .103 .087 175 .135 007 034 .089 .075 175 .135 006 029 .077 .064 180 .116 005 | | | | | | |
| 115 .708 022 200 .387 .348 120 .626 020 170 .344 .307 125 .552 018 144 .304 .270 130 .485 016 123 .268 .236 135 .425 014 104 .236 .207 140 .371 012 089 .207 .180 145 .323 011 076 .181 .156 150 .281 010 064 .157 .136 155 .244 009 055 .137 .117 160 .211 008 047 .119 .101 165 .182 007 040 .103 .087 170 .157 007 034 .089 .075 175 .135 006 029 .077 .064 180 .116 005 025 .066 .055 185 .100 005 | | | | | | |
| 120 .626 020 170 .344 .307 125 .552 018 144 .304 .270 130 .485 016 123 .268 .236 135 .425 014 104 .236 .207 140 .371 012 089 .207 .180 145 .323 011 076 .181 .156 150 .281 010 064 .157 .136 155 .244 009 055 .137 .117 160 .211 008 047 .119 .101 165 .182 007 040 .103 .087 170 .157 007 034 .089 .075 175 .135 006 029 .077 .064 180 .116 005 025 .066 .055 185 .100 005 022 .057 .047 190 .085 004 | | | | | | |
| 125 .552 018 144 .304 .270 130 .485 016 123 .268 .236 135 .425 014 104 .236 .207 140 .371 012 089 .207 .180 145 .323 011 076 .181 .156 150 .281 010 064 .157 .136 155 .244 009 055 .137 .117 160 .211 008 047 .119 .101 165 .182 007 040 .103 .087 170 .157 007 034 .089 .075 175 .135 007 034 .089 .075 175 .135 006 029 .077 .064 180 .116 005 025 .066 .055 185 .100 005 025 .066 .055 185 .100 004 | | | | | | |
| 130 .485 016 123 .268 .236 135 .425 014 104 .236 .207 140 .371 012 089 .207 .180 145 .323 011 076 .181 .156 150 .281 010 064 .157 .136 155 .244 009 055 .137 .117 160 .211 008 047 .119 .101 165 .182 007 040 .103 .087 170 .157 007 034 .089 .075 175 .135 006 029 .077 .064 180 .116 005 025 .066 .055 185 .100 005 022 .057 .047 190 .085 004 019 .049 .040 195 .073 004 014 .035 .029 205 .053 003 | | | | | | |
| 135 .425 014 104 .236 .207 140 .371 012 089 .207 .180 145 .323 011 076 .181 .156 150 .281 010 064 .157 .136 155 .244 009 055 .137 .117 160 .211 008 047 .119 .101 165 .182 007 040 .103 .087 170 .157 007 034 .089 .075 175 .135 006 029 .077 .064 180 .116 005 025 .066 .055 185 .100 005 025 .066 .055 185 .100 005 022 .057 .047 190 .085 004 019 .049 .040 195 .073 004 014 .035 .029 205 .053 003 | | | | | | |
| 140 .371 012 089 .207 .180 145 .323 011 076 .181 .156 150 .281 010 064 .157 .136 155 .244 009 055 .137 .117 160 .211 008 047 .119 .101 165 .182 007 040 .103 .087 170 .157 007 034 .089 .075 175 .135 006 029 .077 .064 180 .116 005 025 .066 .055 185 .100 005 022 .057 .047 190 .085 004 019 .049 .040 195 .073 004 019 .049 .040 195 .073 004 014 .035 .029 205 .053 003 012 .030 .025 210 .045 003 | | | | | | |
| 145 .323 011 076 .181 .156 150 .281 010 064 .157 .136 155 .244 009 055 .137 .117 160 .211 008 047 .119 .101 165 .182 007 040 .103 .087 170 .157 007 034 .089 .075 175 .135 006 029 .077 .064 180 .116 005 025 .066 .055 185 .100 005 022 .057 .047 190 .085 004 019 .049 .040 195 .073 004 019 .049 .040 195 .073 004 014 .035 .029 205 .053 003 012 .030 .025 210 .045 003 010 .026 .021 215 .038 003 | | | | | | |
| 150 .281 010 064 .157 .136 155 .244 009 055 .137 .117 160 .211 008 047 .119 .101 165 .182 007 040 .103 .087 170 .157 007 034 .089 .075 175 .135 006 029 .077 .064 180 .116 005 025 .066 .055 185 .100 005 022 .057 .047 190 .085 004 019 .049 .040 195 .073 004 019 .049 .040 195 .073 004 014 .035 .029 205 .053 003 012 .030 .025 210 .045 003 012 .030 .025 210 .045 003 010 .026 .021 225 .028 002 | | | | | | |
| 155 .244 009 055 .137 .117 160 .211 008 047 .119 .101 165 .182 007 040 .103 .087 170 .157 007 034 .089 .075 175 .135 006 029 .077 .064 180 .116 005 025 .066 .055 185 .100 005 022 .057 .047 190 .085 004 019 .049 .040 195 .073 004 016 .042 .034 200 .062 004 014 .035 .029 205 .053 003 012 .030 .025 210 .045 003 012 .030 .025 215 .038 003 009 .022 .018 220 .033 002 008 .019 .015 225 .028 002 | | | | | | |
| 160 .211 008 047 .119 .101 165 .182 007 040 .103 .087 170 .157 007 034 .089 .075 175 .135 006 029 .077 .064 180 .116 005 025 .066 .055 185 .100 005 022 .057 .047 190 .085 004 019 .049 .040 195 .073 004 016 .042 .034 200 .062 004 014 .035 .029 205 .053 003 012 .030 .025 210 .045 003 010 .026 .021 215 .038 003 009 .022 .018 220 .033 002 008 .019 .015 225 .028 002 007 .016 .013 | | | | | | |
| 165 .182 007 040 .103 .087 170 .157 007 034 .089 .075 175 .135 006 029 .077 .064 180 .116 005 025 .066 .055 185 .100 005 022 .057 .047 190 .085 004 019 .049 .040 195 .073 004 016 .042 .034 200 .062 004 014 .035 .029 205 .053 003 012 .030 .025 210 .045 003 012 .030 .025 215 .038 003 009 .022 .018 220 .033 002 008 .019 .015 225 .028 002 007 .016 .013 | | | | | | |
| 170 .157 007 034 .089 .075 175 .135 006 029 .077 .064 180 .116 005 025 .066 .055 185 .100 005 022 .057 .047 190 .085 004 019 .049 .040 195 .073 004 016 .042 .034 200 .062 004 014 .035 .029 205 .053 003 012 .030 .025 210 .045 003 012 .030 .025 215 .038 003 009 .022 .018 220 .033 002 008 .019 .015 225 .028 002 007 .016 .013 | | | | | | |
| 175 .135 006 029 .077 .064 180 .116 005 025 .066 .055 185 .100 005 022 .057 .047 190 .085 004 019 .049 .040 195 .073 004 016 .042 .034 200 .062 004 014 .035 .029 205 .053 003 012 .030 .025 210 .045 003 012 .030 .025 215 .038 003 009 .022 .018 220 .033 002 008 .019 .015 225 .028 002 007 .016 .013 | | | | | | |
| 180 .116 005 025 .066 .055 185 .100 005 022 .057 .047 190 .085 004 019 .049 .040 195 .073 004 016 .042 .034 200 .062 004 014 .035 .029 205 .053 003 012 .030 .025 210 .045 003 012 .030 .025 215 .038 003 009 .022 .018 220 .033 002 008 .019 .015 225 .028 002 007 .016 .013 | | | | | | |
| 185 .100 005 022 .057 .047 190 .085 004 019 .049 .040 195 .073 004 016 .042 .034 200 .062 004 014 .035 .029 205 .053 003 012 .030 .025 210 .045 003 010 .026 .021 215 .038 003 009 .022 .018 220 .033 002 008 .019 .015 225 .028 002 007 .016 .013 | | | | | | |
| 190 .085 004 019 .049 .040 195 .073 004 016 .042 .034 200 .062 004 014 .035 .029 205 .053 003 012 .030 .025 210 .045 003 010 .026 .021 215 .038 003 009 .022 .018 220 .033 002 008 .019 .015 225 .028 002 007 .016 .013 | | | | | | |
| 195 .073 004 016 .042 .034 200 .062 004 014 .035 .029 205 .053 003 012 .030 .025 210 .045 003 010 .026 .021 215 .038 003 009 .022 .018 220 .033 002 008 .019 .015 225 .028 002 007 .016 .013 | | | | | | |
| 200 .062 004 014 .035 .029 205 .053 003 012 .030 .025 210 .045 003 010 .026 .021 215 .038 003 009 .022 .018 220 .033 002 008 .019 .015 225 .028 002 007 .016 .013 | | | | | | |
| 210 .045 003 010 .026 .021 215 .038 003 009 .022 .018 220 .033 002 008 .019 .015 225 .028 002 007 .016 .013 | 200 | .062 | 004 | | .035 | .029 |
| 210 .045 003 010 .026 .021 215 .038 003 009 .022 .018 220 .033 002 008 .019 .015 225 .028 002 007 .016 .013 | | | | | | |
| 215 .038 003 009 .022 .018 220 .033 002 008 .019 .015 225 .028 002 007 .016 .013 | | | | | | |
| 220 .033002008 .019 .015 225 .028002007 .016 .013 | | | | | | |
| - " | 220 | .033 | 002 | | .019 | .015 |
| 230 .023002006 .013 .011 | 225 | .028 | 002 | 007 | .016 | .013 |
| | 230 | .023 | 002 | 006 | .013 | .011 |

| | _ | | _ | | |
|------|---|----|---|-----|-------|
| TABL | • | 11 | T | | + 1 4 |
| INDL | | 11 | 1 | COL | ıLu |

| time | ^u 7 | u ₈ | TC | F ^C | F ^C 2 |
|-----------|----------------|----------------|-----|----------------|------------------|
| 235 | .020 | 002 | 005 | .011 | .009 |
| 240 | •017 | 002 | 004 | .010 | .008 |
| 245 | .014 | 001 | 004 | .008 | .006 |
| 250 | .012 | 001 | 003 | .007 | .005 |
| 255 | .010 | 001 | 003 | .006 | .005 |
| 260 | .008 | 001 | 002 | .005 | .004 |
| 265 | •007 | 001 | 002 | .004 | .003 |
| 270 | .006 | 001 | 002 | .003 | .003 |
| 275 | .005 | 001 | 002 | .003 | .002 |
| 280 | .004 | 001 | 001 | .002 | .002 |
| 285 | .004 | 001 | 001 | .002 | .002 |
| 290 | .003 | 001 | 001 | .002 | .001 |
| 295 ?? | .002 | 001 | 001 | .001 | .001 |

Note: This table of universal joint control torques and constraint loads applies to the case of feedback control with uncoupled momentum wheels.

TABLE IV.

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| time | u ₇ | u ₈ | TC | F ^C | F ^C ₂ |
|------------|----------------|----------------|------------|----------------|-----------------------------|
| 0 | -1.500 | 192 | .000 | .613 | 576 |
| 5 | 822 | 242 | 984 | •503 | 225 |
| 10 | 176 | 267 | -1.576 | .631 | .097 |
| 15 | .399 | 274 | -1.897 | .759 | .374 |
| 20 | .884 | 267 | -2.032 | .859 | .601 |
| 25 | 1.273 | 251 | -2.043 | .935 | .778 |
| 30 | 1.568 | -,230 | -1.973 | • 993 | ,907 |
| 35 | 1.777 | 207 | -1.853 | 1.033 | .992 |
| 40 | 1.909 | 183 | -1.705 | 1.056 | 1.041 |
| 45 | 1.976 | 161 | -1.545 | 1.061 | 1.058 |
| 50 | 1.989 | 140 | -1.382 | 1.051 | 1.050 |
| 55 | 1.959 | 121 | -1.224 | 1.027 | 1.023 |
| 60 | 1.895 | 104 | -1.076 | • 990 | .981 |
| 65 | 1.808 | 090 | 939 | .945 | .928 |
| 70 | 1.703 | 077 | 815 | .892 | .869 |
| 75 | 1.588 | 067 | 704 | .835 | .806 |
| 80 | 1 - 468 | 058 | 606 | • 775 | .741 |
| 85 | 1.346 | 050 | 520 | •714 | .676 |
| 90 | 1.226 | 043 | 445 | · 654 | .613 |
| 95 | 1.109 | 038 | 380 | •595 | .553 |
| 100 | .998 | 033 | 324 | •538 | .496 |
| 105 | ·894 | 029 | 276 | .484 | .443 |
| 110 | •797 | 025 | 235 | • 434 707 | .393 |
| 115 | .708 | 022 | -,200 | •387 | .348 |
| 120 125 | +626 553 | 020 | 170 | .344 .304 | .307 .270 |
| 130 | .552 .485 | 018 | 144 123 | .268 | .276 |
| 135 | .425 | 016 014 | 104 | .236 | .207 |
| 140 | .371 | 014 | 089 | .207 | .180 |
| 145 | .323 | 011 | 076 | .181 | .156 |
| 150 | .281 | 010 | 064 | .157 | .136 |
| 155 | .244 | 009 | 055 | .137 | .117 |
| 160 | .211 | 008 | 047 | .119 | .101 |
| 165 | .182 | 007 | 040 | .103 | .087 |
| 170 | .157 | 007 | 034 | .089 | .075 |
| 175 | .135 | 006 | 029 | .077 | .064 |
| 180 | .116 | 005 | 025 | .066 | .055 |
| 185 | .100 | 005 | 022 | •057 | .047 |
| 190 | .085 | 004 | 019 | .049 | .040 |
| 195 | .073 | 004 | 016 | .042 | .034 |
| 200 | .062 | 004 | 014 | .035 | .029 |
| 205 | .053 | 003 | 012 | .030 | .025 |
| 210 | .045 | 003 | 010 | .026 | .021 |
| 215 | .038 | 003 | 009 | .022 | .018 |
| 220 | .033 | 002 | 008 | .019 | .015 |
| 225 | .028 | 002 | 007 | .016 | .013 |
| 230 | .023 | 002 | 006 | .013 | .011 |

| | | TABLE IV | . cont'd | | |
|-----------|----------------|----------------|----------|----------------|-----------|
| time | u ₇ | u ₈ | TC | F ^C | F_2^{C} |
| 235 | .020 | 002 | 005 | .011 | .009 |
| 240 | .017 | 002 | 004 | .010 | .008 |
| 245 | .014 | 001 | 004 | .008 | .006 |
| 250 | .012 | 001 | 003 | .007 | .005 |
| 255 | .010 | 001 | 003 | .006 | .005 |
| 260 | .008 | 001 | 002 | .005 | .004 |
| 265 | .007 | 001 | 002 | .004 | .003 |
| 270 | +006 | 001 | 002 | .003 | .003 |
| 275 | .005 | 001 | 002 | .003 | .002 |
| 280 | .004 | 001 | 001 | .002 | .002 |
| 285 | .004 | 001 | 001 | .002 | .002 |
| 290 | .003 | 001 | 001 | .002 | .001 |
| 295 ?? | .002 | 001 | 001 | .001 | .001 |

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Note: This table of universal joint control torques and constraint loads applies to the case of feedback control with the b₂ momentum wheel coupled.

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| time | u ₁ | u ₂ | u ₃ | u ₅ | 2 |
|------------|----------------|----------------|----------------|----------------|--------------|
| 0 | -1.732 | 066 | .180 | .000 | .000 |
| 5 | ,960 | -1.209 | .182 | .096 | .005 |
| 10 | 242 | -1.906 | .205 | .157 | .016 |
| 15 | .382 | -2.296 | .238 | .191 | .032 |
| 20 | .893 | -2.473 | .269 | .206 | .051 |
| 25 | 1.286 | -2.504 | .291 | .207 | .069 |
| 30 | 1.566 | -2.438 | .301 | .199 | .088 |
| 35 | 1.744 | -2.311 | • 299 | .184 | .105 |
| 40 | 1.832 | -2.147 | .287 | .165 | .121 |
| 45 | 1.845 | -1.964 | .268 | .145 | .135 |
| 50 | 1.799 | -1.777 | .244 | .123 | .148 |
| 55 | 1.706 | -1.593 | .218 | .102 | .158 |
| 60 | 1.579 | -1.418 | .192 | .082 | .166 |
| 65 | 1.430 | -1.256 | .167 | .062 | .173 |
| 70 | 1.267 | -1.108 | .144 | .045 | .178 |
| 75 | 1.098 | 974 | .122 | .028 | .181 |
| 80 | •929 | 855 | .104 | .014 | .183 |
| 85 | 764 | 750 | •088 | .001 | .183 |
| 90 | •607 | 657 | .074 | 010 | .183 |
| 95 | .461 | 576 | .062 | 019 | .182 |
| 100 | ·325 | • 506 | .052 | 028 | .180 |
| 105 | .203 | - • 445 | .044 | 035 | .177 |
| 110 | .093 | 392 | .037 | 040 | .173 |
| 115 | 005 | -,346 | .032 | 045 | .169 |
| 120 125 | 090 147 | 306 | +027 | 048 | .165 |
| 130 | 163 226 | 271 242 | .023 | 051 | .161 |
| 135 | 278 | 242 216 | .020 .017 | 053 055 | .156 .151 |
| 140 | 322 | 194 | .015 | 056 | .146 |
| 145 | 357 | 174 | .013 | 056 | .141 |
| 150 | 385 | 157 | .011 | 056 | .136 |
| 155 | 406 | 142 | .010 | 056 | .131 |
| 160 | 422 | 129 | .009 | 055 | .126 |
| 165 | 433 | 118 | .008 | 054 | .121 |
| 170 | 439 | 108 | .007 | 053 | .116 |
| 175 | 441 | 099 | •006 | 052 | .111 |
| 180 | 441 | 091 | .006 | 051 | .106 |
| 185 | 437 | 084 | .005 | 049 | .102 |
| 190 | 432 | 077 | .004 | 048 | .097 |
| 195 | 424 | 072 | .004 | 046 | .093 |
| 200 | 416 | 067 | .004 | 045 | .089 |
| 205 | 405 | 062 | .003 | 043 | .085 |
| 210 | 394 | 058 | .003 | 041 | .081 |
| 215 | 383 | 054 | .003 | 040 | •077 |
| 220 | 371 | 050 | .002 | 038 | .074 |
| 225 | 358 | 047 | .002 | 037 | .070 |
| 230 | 345 | 044 | .002 | 035 | .067 |
| | | | | | |

TABLE V. cont'd

| time | u ₁ | u ₂ | u ₃ | u ₅ | 2 |
|-------------------|----------------|----------------|----------------|----------------|------|
| 235 | 333 | 041 | .002 | 034 | .064 |
| 240 | -,320 | 039 | .002 | 032 | .061 |
| 245 | 307 | 037 | .001 | 031 | .058 |
| 250 | 295 | 035 | .001 | 030 | .055 |
| 255 | 283 | 033 | .001 | 028 | .053 |
| 260 | 271 | 031 | .001 | 027 | .050 |
| 265 | 259 | 029 | .001 | 026 | .048 |
| 270 | 248 | 027 | .001 | 025 | .046 |
| 275 | 237 | 026 | .001 | 023 | .043 |
| 280 | 226 | 024 | .001 | 022 | .041 |
| 285 | 216 | 023 | .001 | 021 | .039 |
| 290 | 206 | 022 | .001 | 020 | .037 |
| 29 5 ?? | 197 | 021 | .001 | 019 | .036 |

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Note: This table of thruster torques u_1 , u_2 , and u_3 and wheel torque u_5 applies to the case of feedback control with u_5 the u_2 momentum wheel coupled.

TABLE VI.

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| | | , , , , | | | |
|------|----------------|----------------|--------|----------------|----------------|
| time | u ₇ | ^u 8 | TC | F ^C | F ^C |
| 0 | -1.500 | 192 | .021 | .612 | -,500 |
| 5 | 830 | 281 | 471 | .340 | -,225 |
| 10 | 403 | 314 | 738 | .242 | 074 |
| 15 | 201 | -,298 | 882 | .223 | 071 |
| 20 | 180 | 251 | 974 | •237 | 124 |
| 25 | 285 | 192 | -1.054 | .288 | 223 |
| 30 | 463 | 136 | -1.139 | •379 | 346 |
| 35 | 671 | 093 | -1.231 | .495 | 476 |
| 40 | 878 | 068 | -1.323 | .619 | -,602 |
| 45 | -1.067 | 063 | -1.402 | .740 | 721 |
| 50 | -1.230 | 074 | -1.454 | •851 | 831 |
| 55 | -1.371 | 095 | -1.470 | • 953 | -,936 |
| 60 | -1.499 | 119 | -1.444 | 1.051 | -1.038 |
| 65 | -1.629 | 139 | -1.379 | 1.150 | -1.141 |
| 70 | -1.771 | 151 | -1.280 | 1.253 | -1.248 |
| 75 | -1.933 | 151 | -1.159 | 1.363 | -1.359 |
| 80 | -2.119 | 141 | -1.029 | 1.478 | -1.473 |
| 85 | -2.322 | 122 | 900 | 1.596 | -1.589 |
| 90 | -2.537 | 099 | 784 | 1.712 | -1.704 |
| 95 | -2.751 | 075 | 687 | 1.822 | -1.813 |
| 100 | -2.954 | 054 | 612 | 1.922 | -1.914 |
| 105 | -3.139 | 036 | 559 | 2.012 | -2,003 |
| 110 | -3.300 | 024 | 524 | 2.088 | -2,080 |
| 115 | -3,433 | 016 | 504 | 2.152 | -2.143 |
| 120 | -3.541 | 011 | 492 | 2.204 | -2.194 |
| 125 | -3.626 | 010 | -,483 | 2.245 | -2,235 |
| 130 | -3.693 | 010 | 473 | 2.27 9 | -2,268 |
| 135 | -3.746 | 010 | 458 | 2.306 | -2,295 |
| 140 | -3.792 | 010 | 440 | 2.330 | -2.318 |
| 145 | -3.834 | 009 | 416 | 2.351 | -2.338 |
| 150 | -3.873 | 008 | 391 | 2.371 | -2.357 |
| 155 | -3.912 | 005 | 364 | 2.389 | -2.375 |
| 160 | -3.950 | 003 | 340 | 2.407 | -2.392 |
| 165 | -3.986 | .000 | 318 | 2.423 | -2,408 |
| 170 | -4.020 | .003 | 301 | 2.437 | -2.422 |
| 175 | -4.049 | .005 | 288 | 2.449 | -2,434 |
| 180 | -4.072 | .006 | 280 | 2.458 | -2.443 |
| 185 | -4.090 | •007 | 276 | 2.465 | -2,449 |
| 190 | -4.103 | .007 | 274 | 2 + 469 | -2.453 |
| 195 | -4.110 | .006 | 273 | 2.471 | -2,455 |
| 200 | -4.113 | .006 | 272 | 2.471 | -2,455 |
| 205 | -4.114 | .005 | 271 | 2.470 | -2.454 |
| 210 | -4.112 | .004 | 269 | 2 • 469 | -2.452 |
| 215 | -4.110 | .003 | 266 | 2.466 | -2.450 |
| 220 | -4.107 | .003 | 262 | 2.464 | -2.447 |
| 225 | -4.104 | .003 | 258 | 2.461 | -2,445 |
| 230 | -4.101 | •003 | 253 | 2,459 | -2.442 |

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| time | u ₇ | u ₈ | T ^C | F ^C | F ^C ₂ |
|-----------|----------------|----------------|----------------|----------------|-----------------------------|
| 235 | -4.099 | .003 | 249 | 2.456 | -2.440 |
| 240 | -4.096 | .003 | -,246 | 2.453 | -2.437 |
| 245 | -4.093 | .003 | 243 | 2.450 | -2.434 |
| 250 | -3.847 | .003 | -2,162 | 2.495 | -2.284 |
| 255 | -3.192 | .003 | -1.813 | 2.072 | -1.896 |
| 260 | -2.643 | .004 | -1.519 | 1.720 | -1.572 |
| 265 | -2.194 | .005 | -1.276 | 1.432 | -1.306 |
| 270 | -1.824 | .005 | -1.075 | 1.194 | -1.087 |
| 275 | -1.519 | .006 | 907 | •998 | -,906 |
| 280 | -1.267 | •006 | 768 | .836 | 757 |
| 285 | -1.059 | .006 | 651 | .702 | 634 |
| 290 | 887 | .006 | 553 | .590 | 532 |
| 295 ?? | 743 | .006 | 471 | .497 | 446 |

Note: This table of universal joint control torques and constraint loads applies to the case of feedback with control torques \mathbf{u}_7 and \mathbf{u}_8 only until \mathbf{t} = 250 seconds, at which time the complete control vector \mathbf{u} is fed back.

TABLE VII.

| time | ω ₀₁ | ω_{02} | ω_{03} | Ÿ ₄ | \dot{y}_5 |
|------------|------------------------|---------------|---------------|----------------|-------------|
| 0 | .000 | .000 | .102 | .000 | .009 |
| 5 | .001 | .001 | .102 | 003 | +008 |
| 1.0 | .001 | .002 | .102 | 004 | .006 |
| 15 | •000 | .003 | .102 | 004 | .005 |
| 20 | 001 | .004 | .102 | 003 | .004 |
| 25 | 002 | .004 | .101 | -,002 | .003 |
| 30 | 004 | .004 | .101 | 001 | .003 |
| 35 | 005 | .004 | .101 | .000 | .002 |
| 40 | 005 | .003 | .101 | .000 | .002 |
| 45 | 005 | .002 | .101 | .000 | .002 |
| 50 | 005 | +002 | .101 | 001 | .001 |
| 55 | 004 | .001 | .101 | 002 | .001 |
| 60 | 003 | .002 | .101 | 003 | .001 |
| 65 | 002 | .002 | .101 | 004 | .001 |
| 70 | 001 | .003 | .101 | 004 | .000 |
| 75 | .000 | .004 | .101 | 005 | .000 |
| 80 | .000 | .005 | .101 | 004 | 001 |
| 85 | .000 | .006 | .101 | 004 | 001 |
| 90 | .000 | .007 | .101 | 004 | 001 |
| 95 | .000 | •008 | .101 | 003 | 001 |
| 100 | 001 | .008 | .101 | 002 | 002 |
| 105 | 001 | .009 | .101 | 002 | 002 |
| 110 | 001 | •009 | .101 | 001 | 002 |
| 115 | 001 | .009 | .101 | 001 | 002 |
| 120 | 001 | .009 | .101 | 001 | 002 |
| 125 | 001 | .009 | .101 | 001 | 002 |
| 130 | 001 | .009 | .101 | 001 | 002 |
| 135 | 001 | .009 | .101 | 001 | 002 |
| 140 | 001 | •009 | .101 | 001 | 002 |
| 145 | 001 | •009 | .101 | 001 | 002 |
| 150 | 001 | .010 | .101 | 001 | 002 |
| 155 | .000 | .010 | .101 | 001 | 002 |
| 160 | .000 | .010 | .101 | 001 | 002 |
| 165 | 001 | .010 | .101 | 001 | 001 |
| 170 | 001 | .010 | .101 | .000 | 001 |
| 175 | 001 | .010 | .101 | .000 | -,001 |
| 180 | 001 | .010 | .101 | .000 | 001 |
| 185 | 001 | .010 | .101 | .000 .000 | 001 001 |
| 190 | 001 | .010 | .101 | | |
| 195 | 001 | .010 | .101 | .000 | 001 001 |
| 200 | 001 | .010 | .101 | .000 .000 | 001 |
| 205 210 | 001 | .010 | .101 .101 | .000 | 001 |
| 210 | 001 001 | .010 | .101 | .000 | 001 |
| 220 | 001 | .010 .010 | .101 | .000 | 001 |
| 225 | 001 | .010 | .101 | .000 | 001 |
| 230 | 001 | .010 | .101 | .000 | 001 |
| 230 | + 0.0 T | +010 | +101 | • • • • | .001 |

TABLE VII. cont'd

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| time | $oldsymbol{\omega}_{01}$ | ω_{02} | ω_{03} | γ ₄ | γ ₅ |
|-----------|--------------------------|---------------|---------------|----------------|----------------|
| 235 | 001 | .010 | .101 | .000 | 001 |
| 240 | 001 | .010 | .101 | .000 | 001 |
| 245 | 001 | .010 | .101 | .000 | 001 |
| 250 | 001 | .009 | .101 | .000 | 001 |
| 255 | .000 | •008 | .101 | .000 | 001 |
| 260 | .000 | .006 | .101 | .000 | 001 |
| 265 | •000 | .005 | .101 | .000 | 001 |
| 270 | .000 | .004 | .101 | .000 | 001 |
| 275 | .000 | •003 | .101 | .000 | 001 |
| 280 | .000 | .002 | .101 | .000 | .000 |
| 285 | .000 | .002 | .101 | .000 | .000 |
| 290 | .000 | .002 | .101 | .000 | .000 |
| 295 ?? | .000 | .001 | .101 | .000 | .000 |

NOTE: This table of OMV angular velocity components, target spin rate and precession angle rate of change is for the case of feedback with u7 and u8 control vector components only, until t = 250 seconds when control is with the complete u vector.

V. Conclusion

A nonlinear feedback control law was developed and used to despin and detumble an axially symmetric target satellite originally in steady spin and precession. The control law derivation is based upon Liapunov stability theory, and ensures the global asymptotic stability of the final spin-stabilized equilibrium state. The results indicate that the system is well behaved, in the sense that changes in both the system state and in the control torques are smooth throughout the maneuver. The control torque magnitudes are relatively small, and no extreme loading of the connecting joint between OMV and target satellites occurred. The system could be driven very close to the spin-stabilized state using the joint control torques alone. However, a residual target precession angle remained at the end of the 300 second maneuver, as did non-zero b_1 and b_2 OMY velocity components. This is due to the fact that after approximately 200 seconds of feedback control, the matrix, A, of Eq (26) is nearly diagonal, and as a result the control torques u_7 and u_8 are coupled strongly only to the target precession angle rate and spin rate, and the precession angle (states x_7 , x_8 , and x_9), all of which have very small values. The available control torques at the universal joint are thus insufficient for the reduction of target precession angle at any appreciable rate. Implementation of full vector control (using all eight control torques) at t = 250 seconds successfully drove the system to the spin-stabilized equilibrium.

Although the OMV thrust torque magnitude could be reduced by coupling a momentum wheel torque to the target precession angle, no attempt was made to accomplish detumbling with momentum wheel and joint

torques alone. Any attempt made to couple the b_3 momentum wheel with system states x_7 or x_8 resulted in an increase in at least one thrust torque profile, with no obvious positive influence on system behavior.

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A follow on effort might concentrate on the development of a reliable technique for determining the values of the off-diagonal gain matrix terms, based on desired system response. Then an attempt could be made to perform the bulk of the maneuver using only internal torques.

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VITA

X

Lieutenant Kirk R. Fleming was born on 13 October 1954 in Port Huron, Michigan. He graduated from Port Huron Northern High School in January 1972, and attended the University of Texas at Austin from August 1979 to December 1981, when he received the degree of Bachelor of Science in Aerospace Engineering. He received a commission in the USAF through the Air Force Officer Training School in April 1982. He then served as a research and development project engineer in the Air Force Flight Dynamics Laboratory, Vehicle Equipment Division, Wright-Patterson AFB, Ohio until entering the School of Engineering, Air Force Institute of Technology, in May 1984.

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From Block 19:

The problem of detumbling a freely spinning and precessing axially symmetric satellite is considered. Detumbling is achieved with another axisymmetric orbital maneuvering vehicle (OMV) joined to the target satellite with a universal joint. The joint provides two rotational degrees of freedom and is translated across the surface of the OMV during the detumbling process. The target satellite and the OMV with its three momentum wheels are modelled as a five body system using Eulerian-based equations of motion developed by Hooker and Margulies. A Liapunov technique is applied to derive a nonlinear feedback control law which drives the system asymptotically to a final spin-stabilized state. State and control histories are presented and indicate that the detumbling process is benign. Constraint force and moment loads at the connection between the OMV and target satellites are also presented, and indicate that no extreme loads are encountered during the despinning and detumbling process.

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